## Wormley CE Primary

 School

How we teach mathematics:

# Policy for Mathematics 

September 2017

Take Responsibility, Show Respect, Have Faith and Achieve


#### Abstract

Aims At Wormley CE Primary School, we recognise and promote maths as a creative and interconnected subject. We believe that everybody is capable of being a successful mathematician. The subject is essential to everyday life and provides a foundation for understanding the world. Our aim is to provide our learners with rich opportunities in maths to learn independently and actively in order that they: - Become fluent in the fundamentals of mathematics: - Are able to reason and justify mathematically; - Can solve problems within a range of contexts.

We believe mixed ability group and paired work is vital with a strong emphasis on 'talk' to allow children to 'think aloud' and build the skills necessary to be confident mathematicians. Through varied, engaging and open ended scenarios, which are relevant to the learner, we aim to nurture a love and curiosity of the subject.


## Rationale

This policy has been devised to support these aims and meet the requirements of the National Curriculum 2014 for the teaching and learning of mathematics.
It is also designed to give pupils a consistent and smooth progression of learning, particularly in mental and written calculation, across the school.
Throughout our teaching, we aim to link key manipulatives and representations (for example dienes blocks, numberlines, Numicon, Cuisenaire rods, place value counters) in order that the children can be vertically accelerated through each strand of calculation. We aim to ensure a consistency of approach, enabling children to progress stage by stage through models and representations they recognise from previous teaching, allowing for deeper conceptual understanding and fluency. Key manipulatives and representations are available to children whatever their age or ability. We spend time looking explicitly at common misconceptions and why these may arise.
In addition to the daily maths lesson, maths will be taught across the curriculum to make it meaningful and relevant to learners.
As children are taught at the pace appropriate to them, teachers will be presenting strategies and equipment appropriate to children's level of understanding. It is vital that pupils are taught according to the stage that they are currently working at. Those who grasp concepts rapidly should be challenged through rich and sophisticated problems before being presented with new material; those who are not sufficiently fluent with earlier material will be allowed to consolidate their understanding before moving on. However, it is expected that the majority of children in each class will be working at age-appropriate levels as set out in the National Curriculum 2014.
Please note that early learning in number and calculation in Reception follows the "Development Matters" EYFS document, and this calculation policy is designed to build on progressively from the content and methods established in the Early Years Foundation Stage.

## Teaching Sequence

In further support of our aims, we have adopted a clear teaching sequence (see appendix 1) to support progression through mathematical concepts all of which is delivered within meaningful problem-solving contexts. These were developed with written calculation in mind but apply to all areas of mathematics. We currently follow the Herts for Learning Essentials planning that outlines the
sequences of learning that children should undertake to consolidate their mathematical understanding.

## Mental Mathematics

Progression in mental calculations is detailed in Appendix 2. We recognise the importance of the mental strategies and known facts that form the basis of all calculations. Mental methods and place value must be secure BEFORE written methods are taught and used.
Children will ALWAYS be encouraged to use a mental calculation strategy first, whatever their age or ability; written methods will only be used when needed. We value procedural variation and celebrate different methods of calculating whilst aiming for the most efficient method through noticing the numbers.
The following checklists outline the key skills and number facts that children are expected to develop throughout the school.

To add and subtract successfully, children should be able to:

- count on and back in steps of 1,10 and 100 from any number
- have a secure understanding of place value
- recall all addition pairs to $9+9$ and number bonds to 10
- use near doubles and compensation methods
- recognise addition and subtraction as inverse operations
- add mentally a series of one digit numbers (e.g. $5+8+4$ )
- add and subtract multiples of 10 or 100 using the related addition fact and their knowledge of place value (e.g. $600+700,160-70$ )
- partition 2 and 3 digit numbers into multiples of 100,10 and 1 in different ways
(e.g. partition 74 into $70+4$ or $60+14$ ) and recombine
- use estimation by rounding to check answers are reasonable

To multiply and divide successfully, children should be able to:

- add and subtract accurately and efficiently
- recall multiplication facts to $12 \times 12=144$ and division facts to $144 \div 12=12$
- use multiplication and division facts to estimate how many times one number divides into another etc.
. know the outcome of multiplying by 0 and by 1 and of dividing by 1
- understand the effect of multiplying and dividing whole numbers by 10, 100 and later 1000
- recognise factor pairs of numbers (e.g. that $15=3 \times 5$, or that $40=10 \times 4$ ) and increasingly able to recognise common factors
- derive other results from multiplication and division facts and multiplication and division by 10 or 100 (and later 1000)
- notice and recall with increasing fluency inverse facts
- partition numbers into 100s, 10s and 1s or multiple groupings
- understand how the principles of commutative, associative and distributive laws apply or do not apply to multiplication and division
- understand the effects of scaling by whole numbers and decimal numbers or fractions
- understand correspondence where $n$ objects are related to $m$ objects
- investigate and learn rules for divisibility

Children will be taught and encouraged to select the most appropriate calculation method for the numbers involved.

## APPENDIX 1 <br> WRITTEN CALCULATION

## Progression in addition and subtraction

Addition and subtraction are connected.

| Part | Part |
| :---: | :---: |
| Whole |  |

Addition names the whole in terms of the parts and subtraction names a missing part of the whole.

\begin{tabular}{|c|c|}
\hline Addition \& Subtraction \\
\hline \begin{tabular}{l}
Combining two sets (aggregation) \\
Putting together - two or more amounts or numbers are put together to make a total \(7+5=12\)
\[
\begin{array}{cccc}
\mathrm{O}^{\mathrm{O}} \mathrm{O}_{\mathrm{O}}^{\mathrm{O}} \& \mathrm{O} \& \mathrm{O}_{\mathrm{O}}^{\mathrm{O}} \mathrm{O} \longrightarrow \mathrm{O}_{\mathrm{OO}}^{\mathrm{O}} \mathrm{O}_{\mathrm{O}}^{\mathrm{O}} \\
\mathrm{O}^{\mathrm{O}}
\end{array}
\] \\
Count one set, then the other set. Combine the sets and count again. Starting at 1. \\
Counting along the bead bar, count out the 2 sets, then draw them together, count again. Starting at 1.
\end{tabular} \& \begin{tabular}{l}
Taking away (separation model) \\
Where one quantity is taken away from another to calculate what is left.
\[
7-2=5
\]

<br>
Multilink towers - to physically take away objects.
\end{tabular} <br>

\hline \begin{tabular}{l}
Combining two sets (augmentation) \\
This stage is essential in starting children to calculate rather than counting Where one quantity is increased by some amount. Count on from the total of the first set, e.g. put 3 in your head and count on 2 . Always start with the largest number. Counters:
\end{tabular} \& \begin{tabular}{l}
Finding the difference (comparison model) \\
Two quantities are compared to find the difference.
\[
8-2=6
\] \\
Counters:
\(\rightarrow 0\)
\(\rightarrow 0\)

\end{tabular} <br>

\hline
\end{tabular}



Start with 7, then count on $8,9,10,11,12$
Bead strings:


Make a set of 7 and a set of 5 . Then count on from 7.

Multilink Towers:

Cuisenaire Rods:


Number tracks:



Start on 5 then count on 3 more

Bead strings:


Make a set of 8 and a set of 2 . Then count the gap.

Multilink Towers:


Cuisenaire Rods:


Number tracks:
(1) (2) (3) $5 \sqrt{6} 78910 / 11 / 12 / 13 / 14 / 15 / 1617181920$


Start with the smaller number and count the gap to the larger number.

## 1 set within another (part-whole model)

The quantity in the whole set and one part are known, and may be used to find out how many are in the unknown part.
$8-2=6$
Counters:
$\circ$
0
0
Bead strings:
$\square$

## Bridging through 10s

This stage encourages children to become more efficient and begin to employ known facts.

## Bead string:


$7+5$ is decomposed / partitioned into $7+3+2$. The bead string illustrates 'how many more to the next multiple of 10?' (children should identify how their number bonds are being applied) and then 'if we have used 3 of the 5 to get to 10 , how many more do we need to add on? (ability to decompose/partition all numbers applied)

Number track:
$\begin{array}{llllllllll}\text { (1) } & 2 & 3 & 5 & 6 & 7 & 9 & 10 & 11 & 12 \\ 13) & 14 & 15 & 17 & 18 & 19 & 20\end{array}$

Steps can be recorded on a number track alongside the bead string, prior to transition to number line.

Number line


## Bead string:


$12-7$ is decomposed / partitioned in $12-2-5$. The bead string illustrates 'from 12 how many to the last/previous multiple of 10?' and then 'if we have used 2 of the 7 we need to subtract, how many more do we need to count back? (ability to decompose/partition all numbers applied)

Number Track:


Steps can be recorded on a number track alongside the bead string, prior to transition to number line.

## Number Line:



## Counting up or 'Shop keepers' method

## Bead string:


$12-7$ becomes $7+3+2$.
Starting from 7 on the bead string 'how many more to the next multiple of 10?' (children should recognise how their number bonds are being applied), 'how many more to get to 12?'.

## Number Track:



Number Line:



## Working with larger numbers

Tens and ones + tens and ones
Ensure that the children have been transitioned onto Base 10 equipment and understand the abstract nature of the single 'tens' sticks and 'hundreds' blocks

Partitioning (Aggregation model)
$34+23=57$
Base 10 equipment:


Children create the two sets with Base 10 equipment and then combine; ones with ones, tens with tens.

## Partitioning (Augmentation model)

Base 10 equipment:
Encourage the children to begin counting from the first set of ones and tens, avoiding counting from 1. Beginning with the ones in preparation for formal columnar method.


Number line:

Take away (Separation model)
$57-23=34$

## Base 10 equipment:

Children remove the lower quantity from the larger set, starting with the ones and then the tens. In preparation for formal decomposition.


Number Line:


At this stage, children can began to use an informal method to support, record and explain

|  | their method (optional) $(50+7) ;(20,+3)$ |
| :---: | :---: |
| At this stage, children can begin to use an informal method to support, record and explain their method. (optional) |  |

## Bridging with larger numbers

Once secure in partitioning for addition, children begin to explore exchanging. What happens if the ones are greater than 10? Introduce the term 'exchange'. Using the Base 10 equipment, children exchange ten ones for a single tens rod, which is equivalent to crossing the tens boundary on the bead string or number line.

Base 10 equipment:
$37+15=52$


Discuss counting on from the larger number irrespective of the order of the calculation.

Base 10 equipment:
$52-37=15$


## Expanded Vertical Method (optional)

Children are then introduced to the expanded vertical method to ensure that they make the link between using Base 10 equipment, partitioning and recording using this expanded vertical method.

Base 10 equipment:
$67+24=91$


Base 10 equipment:
$91-67=24$



This represents the school's standard written algorithm for addition.

- Start with the least significant digit (ones)
- Carry digits under the answer line
- Place the operation symbol on the left

Consistent wording will be used:
" 7 and 5 is 12, that's 2 ones and carry the ten under the line 6 tens and 8 tens is 14 tens, plus the ten carried across is 15 tens (which is 150)
5 tens stay in the tens column (50) and the hundred is carried under the line
3 hundred plus the hundred carried under the line is 4 hundreds
So, 367 plus 85 equals 452"
so take a ten from the tens column (leaving 6 tens or 60) and exchange it for 10 ones
Now it is 12 ones take away 5 ones, which is 7 ones
Now look at the tens column. 6 tens take away 2 tens is 4 tens
So 72 take away 25 equals 47"

## Vertical acceleration

By returning to earlier manipulative experiences children are supported to make links across mathematics, encouraging 'If I know this...then I also know...' thinking.

## Decimals

Ensure that children are confident in counting forwards and backwards in decimals - using bead strings to support.

## Bead strings:



Each bead represents 0.1 , each different block of colour equal to 1.0
Base 10 equipment:

| $\square$ |  | $\square$ |
| :---: | :---: | :---: |
| 0.1 | 1.0 | 10.0 |

Aggregation $\begin{aligned} & \text { Addition of decimals } \\ & \text { model of addition }\end{aligned}$
Counting both sets - starting at zero.
$0.7+0.2=0.9$
$\begin{array}{lllllll}0.1 & 0.2 & 0.3 & 0.4 & 0.5 & 0.6 & 0.7\end{array}$
$0.8 \quad 0.9$

## Augmentation model of addition

Starting from the first set total, count on to the

## Subtraction of decimals

Take away model
$0.9-0.2=0.7$
$\begin{array}{lllllll}0.1 & 0.2 & 0.3 & 0.4 & 0.5 & 0.6 & 0.7\end{array}$
$0.8 \quad 0.9$
Finding the difference (or comparison model):


## Gradation of difficulty-addition:

1. No exchange
2. Extra digit in the answer
3. Exchanging ones to tens
4. Exchanging tens to hundreds
5. Exchanging ones to tens and tens to hundreds
6. More than two numbers in calculation
7. As 6 but with different number of digits
8. Decimals up to 2 decimal places (same number of decimal places)
9. Add two or more decimals with a range of decimal places

## Gradation of difficulty- subtraction:

1. No exchange
2. Fewer digits in the answer
3. Exchanging tens for ones
4. Exchanging hundreds for tens
5. Exchanging hundreds to tens and tens to ones
6. As 5 but with different number of digits
7. Decimals up to 2 decimal places (same number of decimal places)
8. Subtract two or more decimals with a range of decimal places

## Progression in Multiplication and Division

Multiplication and division are connected.
Both express the relationship between a number of equal parts and the whole.

| Part | Part | Part | Part |
| :---: | :---: | :---: | :---: |
| Whole |  |  |  |

The following array, consisting of four columns and three rows, could be used to represent the number sentences: -
$3 \times 4=12$,
$4 \times 3=12$
$3+3+3+3=12$
$4+4+4=12$.

And it is also a model for division
$12 \div 4=3$
$12 \div 3=4$
$12-4-4-4=0$
$12-3-3-3-3=0$

| Multiplication |  |
| :--- | :---: |
| Early experiences |  |
| Children will have real, practical experiences of |  |
| handling equal groups of objects and counting in |  |
| 2s, 10 s and 5 s . Children work on practical |  |
| problem solving activities involving equal sets or |  |
| groups. |  |
| 10p |  |

## Repeated addition (repeated aggregation)

3 times 5 is $5+5+5=15$ or 5 lots of 3 or $5 \times 3$ Children learn that repeated addition can be shown on a number line.


Children learn that repeated addition can be shown on a bead string.


Children also learn to partition totals into equal trains using Cuisenaire Rods


## Scaling

This is an extension of augmentation in addition, except, with multiplication, we increase the quantity by a scale factor not by a fixed amount. For example, where you have 3 giant marbles and you swap each one for 5 of your friend's small marbles, you will end up with 15 marbles. This can be written as:
$1+1+1=3 \square$ scaled up by $5 \square 5+5+5=15$

For example, find a ribbon that is 4 times as long as the blue ribbon.


We should also be aware that if we multiply by a number less than 1, this would correspond to a scaling that reduces the size of the quantity. For example, scaling 3 by a factor of 0.5 would reduce it to 1.5 , corresponding to $3 \times 0.5=1.5$.

## Sharing equally

6 sweets get shared between 2 people. How many sweets do they each get? A bottle of fizzy drink shared equally between 4 glasses.


## Grouping or repeated subtraction

There are 6 sweets. How many people can have 2 sweets each?


Repeated subtraction using a bead string or number line
$12 \div 3=4$


The bead string helps children with interpreting division calculations, recognising that $12 \div 3$ can be seen as 'how many 3s make 12?' Cuisenaire Rods also help children to interpret division calculations.

|  | Children move onto calculations involving <br> remainders. <br> $13 \div 4=3 r 1$ |
| :--- | :--- | :--- |
| Commutativity |  |
| Children learn that $3 \times 5$ has the same total as 5 | Children learn that division is not commutative |
| $\times 3$. |  |
| This can also be shown on the number line. |  |
| $3 \times 5=15$ |  |
| $5 \times 3=15$ |  |

## Partitioning for multiplication

Arrays are also useful to help children visualise how to partition larger numbers into more useful representation. $9 \times 4=36$


9
Children should be encouraged to be flexible with how they use number and can be encouraged to break the array into more manageable chunks.
$9 \times 4=$


Which could also be seen as
$9 \times 4=(3 \times 4)+(3 \times 4)+(3 \times 4)=12+12+12$
$=36$
Or $3 \times(3 \times 4)=36$
And so $6 \times 14=(2 \times 10)+(4 \times 10)+(4 \times 6)=$ $20+40+24=84$


## Partitioning for division

The array is also a flexible model for division of larger numbers
$56 \div 8=7$


Children could break this down into more manageable arrays, as well as using their understanding of the inverse relationship between division and multiplication. $56 \div 8=(40 \div 8)+(16 \div 8)=5+2=7$

To be successful in calculation learners must have plenty of experiences of being flexible with partitioning, as this is the basis of distributive and associative law.

## Associative law

E.g. $3 \times(3 \times 4)=36$

The principle that if there are

(multiplication only) :three numbers to multiply these can be multiplied in any order.
Distributive law (multiplication):-
E.g. $6 \times 14=(2 \times 10)+(4 \times 10)+(4 \times 6)=20+40+24=84$

This law allows you to distribute a multiplication across an addition or subtraction.

## Distributive law (division):-

E.g. $56 \div 8=(40 \div 8)+(16 \div 8)=5+2=7$

This law allows you to distribute a division across an addition or
 subtraction.


## $24 \times 3$



## Grid method

This written strategy is introduced for the multiplication of TO $\times \mathrm{O}$ to begin with. It may require column addition methods to calculate the total.


Arrays leading into chunking and then long and short division
Children continue to use arrays and partitioning where appropriate, to prepare them for the 'chunking' and short method of division. Arrays are represented as 'grids' as a shorthand version.
e.g. $78 \div 3=$

$78 \div 3=(30 \div 3)+(30 \div 3)+(18 \div 3)=$ $10+10+6=26$
The vertical method- 'chunking' leading to long division
See above for example of how this can be modelled as an array using place value counters. $78 \div 3=$

| 78 |  |
| ---: | ---: |
| $-\quad 30$ |  |
|  | $(10 \times 3)$ |
| $-\quad 30$ | $(10 \times 3)$ |
|  | 18 |
| $-\quad 18$ | $(6 \times 3)$ |

So $78 \div 3=10+10+6=26$

## single digit

The array using place value counters becomes the basis for understanding short multiplication
first without exchange before moving onto exchanging
$24 \times 6$


This represents the school's standard written algorithm for short multiplication.

1. Starting with the least significant digit, in this case ones.
2. Digits carried over should be placed under the answer line.
3. Operation symbol on left

Whereas we can begin to group counters into an array to show short division working $136 \div 4$


This represents the school's standard written algorithm for short division.

Consistent wording will be used:
"4 times 6 units is 24, that's 4 ones and carry the two tens under the line.

6 times 2 tens is 12 tens, plus the 2 tens we carried across makes 14 tens.

That's 4 tens, carry 10 tens (one hundred)
So $24 \times 6=144$."

## Gradation of difficulty (short multiplication)

1. $\mathrm{TO} \times \mathrm{O}$ no exchange
2. $\mathrm{TO} \times \mathrm{O}$ extra digit in the answer
3. TO $\times \mathrm{O}$ with exchange of ones into tens
4. HTO $\times$ O no exchange
5. HTO $\times \mathrm{O}$ with exchange of ones into tens
6. HTO $\times \mathrm{O}$ with exchange of tens into hundreds
7. HTO $\times \mathrm{O}$ with exchange of ones into tens and tens into hundreds
8. As 4-7 but with greater number digits $\times 0$
9. O.t $x \mathrm{O}$ no exchange
10. O.t with exchange of tenths to ones
11. As 9-10 but with greater number of digits which may include a range of decimal places $\times \mathrm{O}$

Start with the most significant digit
"136 divided by 4. How many lots of 4 are there in 136?

There are 30 lots of 4 in 120
There is 4 lots of 4 in 16
So there are 34 lots of 4 in 136"

## Gradation of difficulty (short division)

1. $\mathrm{TO} \div \mathrm{O}$ no exchange no remainder
2. $\mathrm{TO} \div \mathrm{O}$ no exchange with remainder
3. $\mathrm{TO} \div \mathrm{O}$ with exchange no remainder
4. $\mathrm{TO} \div \mathrm{O}$ with exchange, with remainder
5. Zero in the quotient e.g. $816 \div 4=\mathbf{2 0 4}$
6. As $1-5 \mathrm{HTO} \div \mathrm{O}$
7. As 1-5 greater number of digits $\div 0$
8. As 1-5 with a decimal dividend e.g. $7.5 \div 5$ or $0.12 \div 3$
9. Where the divisor is a two digit number

See below for gradation of difficulty with remainders

## Dealing with remainders

Remainders should be given as integers, but children need to be able to decide what to do after division, such as rounding up or down accordingly.
e.g.:

I have 62 p. How many 8 p sweets can I buy?

- Apples are packed in boxes of 8. There are 86 apples. How many boxes are needed?


## Gradation of difficulty for expressing remainders

1. Whole number remainder
2. Remainder expressed as a fraction of the divisor
3. Remainder expressed as a simplified fraction
4. Remainder expressed as a decimal


## Long division -dividing by more than one

## digit

Children should be reminded about partitioning numbers into multiples of $10,100 \mathrm{etc}$. before recording as either:-

1. Chunking model of long division using Base 10 equipment
2. Sharing model of long division using place value counters
See the following pages for exemplification of these methods.

Chunking model of long division using Base 10 equipment
This model links strongly to the array representation; so for the calculation $72 \div 6=$ ? - one side of the array is unknown and by arranging the Base 10 equipment to make the array we can discover this unknown. The written method should be written alongside the equipment so that children make links.


## Begin with divisors that are between 5 and 9

$72 \div 6=12$


1. Make a rectangle where one side is 6 (the number dividing by) - grouping 6 tens

10


60
After grouping 6 lots of 10 (60) we have 12 left over
2. Exchange the remaining ten for ten ones
3.

4. Complete the rectangle by grouping the remaining ones into groups of 6


## Move onto working with divisors between 11

 and 19Children may benefit from practise to make multiples of tens using the hundreds and tens and tens and ones.
$289 \div 12$


1. Make a rectangle where one side is 12 (the number dividing by) using hundreds and tens


With 49 remaining
2. Make groups of 12 using tens and ones


No more groups of 12 can be made and 1 remains


This represents the school's standard written algorithm for long division.

Consistent wording will be used:
"289 divided by 12. How many lots of 12 are there in 289?
$12 \times 10$ is 120 so let's try $12 \times 20$ is 240 .
Take 20 lots of 12 away from 289 (explain the subtraction) this leaves us with $49.12 \times 4$ is 48.49 take away 48 is 1.

|  | 8 is less than 12 so we have a remainder of 1. <br> We took away one chunk of 20 lots of 12 and one <br> chunk of 4 lots of 12. So the answer is 24 remainder <br> $1 . "$ |
| :--- | :--- |

## Sharing model of long division using place value counters

Starting with the most significant digit, share the hundreds. The writing in brackets is for verbal


4


Moving to tens - exchanging hundreds for tens means that we now have a total of 13 tens
4


4 (4 hundredsused)

(13 tens)


4


4

(4 hundreds used)
(13 tens)
(12 tens used)
(1 ten left)
Moving to ones, exchange tens to ones means that we now have a total of 12 ones counters (hence the arrow)
4


4



## Appendix 2 - Mental maths progression

| Strategy | EYFS | KS1 | LKS2 | UKS2 |
| :---: | :---: | :---: | :---: | :---: |
| Counting forwards and backwards |  |  |  |  |
| Count on in ones from 4 or 5 (4+5) | V | * |  |  |
| Count back in ones from 8 (8-3) | $\checkmark$ | * |  |  |
| Count on in ones from 10 or use place value ( $\mathbf{1 0 + 7 )}$ | $\checkmark$ | * |  |  |
| Count on in ones from 13 (13+5) | V | * |  |  |
| Count back in ones from 17 (17-3) | V | * |  |  |
| Count back in twos (18-6) |  | V | * |  |
| Count on in ones from 23 (23+5) |  | $\checkmark$ | * |  |
| Count back in ones from 57 (57-3) |  | V | * |  |
| Count on in ones or use place value ( $60+5$ ) |  | $\checkmark$ | * |  |
| Count back in ones from 80 or use known number facts and place value ( $80-7$ ) |  | v | * |  |
| Count on in tens from $27(27+60)$ |  | $\checkmark$ | * | * |
| Count back in tens from 72 (72-50) |  | V | * | * |
| Count on in tens then in ones from $50(50+38)$ |  | $\checkmark$ | * | * |
| Count back in tens then in ones from 90 (90-27) |  | $\checkmark$ | * | * |
| Count on in tens then ones from $34(34+65)$ |  | V | * | * |
| Count back in tens then ones from 87 (87-23) |  | $\checkmark$ | * | * |
| Count on in steps of 5 from $35(35+15)$ |  | $\checkmark$ | * | * |
| Count up from 68, counting 2 to 70 then 3 to 73 (73-68) |  | $\checkmark$ | * | * |
| Count on 50 from 47, then 3 to 100, then 5 to 105 (47 + 58) |  | $\checkmark$ | * | * |
| Count back from 40 from 124, then 4 to 80, then 3 to 77 (124 47) |  |  | V | * |
| Count on in hundreds from 570 (570 + 300) |  |  | V | * |
| Count back in hundreds from 960 (960-500) |  |  | $\checkmark$ | * |
| Count on in tenths (3.2+0.6) |  |  | $\checkmark$ | * |
| Count on in tenths and hundredths (1.7 + 0.55) |  |  | $\checkmark$ | * |

V - To be introduced in this phase

*     - To be practised and revised in this phase

| Strategy | EYFS | KS1 | LKS2 | UKS2 |
| :---: | :---: | :---: | :---: | :---: |
| Doubling and halving |  |  |  |  |
| Double all numbers to 10 (double 9) | V | * |  |  |
| Double all numbers to 20 and find corresponding halves (double 7, half of 14) | V | * |  |  |
| Double multiples of 10 to 50 and find corresponding halves (double 40) |  | V | * |  |
| Double multiples of 5 to 50 and find the corresponding halves (double 35, half of 70 ) |  | V | * |  |
| Double multiples of 10 to 100 and their corresponding halves (double 90, half of 180) |  | V | * |  |
| Double multiples of 5 to 100 and find the corresponding halves (double 85, half of 170) |  |  | V | * |
| Double any two-digit number and find the corresponding halves (double 47, half of 94) |  |  | V | * |
| Double multiples of 10 and 100 and find the corresponding halves (double 800/half of $\mathbf{1 6 0 0}$, double $\mathbf{3 4 0}$ /half of $\mathbf{6 8 0}$ ) |  |  | V | * |
| Use doubling and halving when calculating up to $\times 10$ (x 4 double twice, $\times 8$ - double three times and vice versa) |  |  | V | * |
| Multiply by 20 by doubling and multiplying by 10 ( $\mathbf{5 3} \times \mathbf{2 0}=\mathbf{5 3} \times$ $2=106,106 \times 10=1060$ ) |  |  | V | * |
| Multiply by 50 by multiplying by 100 then halving ( $\mathbf{7 3 \times 5 0 = 7 3 \times}$ $100=7300,7300 \div \mathbf{2}=\mathbf{3 6 5 0}$ ) |  |  | V | * |
| Multiply by 25 by multiplying by 100 then halving twice ( $\mathbf{6 2 \times 2 5}$ $=62 \times 100=6200,6200 \div 2=3100,3100 \div 2=1550$ ) |  |  |  | V |
| Double decimal fractions with ones and tenths and find the corresponding halves (double 7.6, half of 15.2) |  |  |  | V |
| Divide by 50 by dividing by 100 then doubling ( $\mathbf{2 7 0} \div \mathbf{5 0}=\mathbf{2 . 7} \mathbf{x} \mathbf{2}$ = 5.4) |  |  |  | V |
| Divide by 25 by dividing by 100 then multiplying by $4 \mathbf{( 4 6 0} \div \mathbf{2 5}=$ $4.6 \times 4=18.4$ ) |  |  |  | V |
| Strategy | EYFS | KS1 | LKS2 | UKS2 |
| Partitioning: using near doubles/compensating |  |  |  |  |
| $\mathbf{6 + 7}$ is double 6 add 1 or double 7 subtract 1 |  | $\checkmark$ |  |  |
| $\mathbf{1 3 + 1 4}$ is double 13 add 1 or double 14 subtract 1 |  | V |  |  |
| $\mathbf{3 9 + 4 0}$ is double 40 subtract 1 |  | v | * |  |
| $\mathbf{1 8 + 1 6}$ is double 18 subtract 2 or double 16 add 2 |  | V | * |  |

$60+70$ is double 60 and add 10 or double 70 subtract 10
$76+75$ is double 76 subtract 1 or double 75 add 1
$160+170$ is double 150, add 10, add 20 or double 160 add 10 or double 170 subtract 10
$\mathbf{2 . 5}+\mathbf{2 . 6}$ is double 2.5 add 0.1 or double 2.6 subtract 0.1

|  |  | $\vee$ | $*$ |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  | V | ${ }^{*}$ |
|  |  |  | V | ${ }^{*}$ |
|  |  |  |  | V |


| Strategy | EYFS | KS1 | LKS2 | UKS2 |
| :---: | :---: | :---: | :---: | :---: |
| Partitioning: bridging through multiples of 10 |  |  |  |  |
| 5+8 or 12-7: 5+5+3 or 12-2-5 | V | * |  |  |
| 65 + 7 or 43-6: 65+5+2 or 43-3-3 |  | V | * |  |
| 24-19: 19+1+4 |  | V | * |  |
| 49 + 32: 49+1+31 |  | V | * | * |
| 90-27: 27+3+60 |  |  | V | * |
| 57-34 or 92-25: 57+3+31 or 92-2-20-3 |  |  | V | * |
| 84-35: $35+5+40+4$ |  |  | $\checkmark$ | * |
| 607-288: $288+12+300+7$ |  |  | $\checkmark$ | * |
| 6070-4987: 4987+13+1000+70 |  |  | V | * |
| 1.4 + 1.7 or 5.6-3.7: 1.4+0.6+1.1 or 5.6-0.6-3-0.1 |  |  |  | V |
| 0.8+0.35: 0.8+0.2+0.15 |  |  |  | $\checkmark$ |
| 8.3-2.8: $2.8+0.2+5.3$ or 8.3-2.3-0.5 |  |  |  | $\checkmark$ |


| Strategy | EYFS | KS1 | LKS2 | UKS2 |
| :---: | :---: | :---: | :---: | :---: |
| Partitioning: compensation |  |  |  |  |
| $34+9,34+19,34+29 \text { etc: } 34+10-1,34+20-1,34+30-1$ etc |  | V | * |  |
| $\begin{aligned} & \mathbf{3 4 + 1 1 , 3 4 + 2 1 , 3 4 + 3 1} \text { etc: } 34+10+1,30+20+1,34+30+1 \\ & \text { etc } \end{aligned}$ |  | V | * |  |
| 70-9: 70-10+1 |  | V | * |  |
| 53+12: $53+10+2$ |  | $\checkmark$ | * |  |
| 53-12: 53-10-2 |  | $\checkmark$ | * |  |
| 53 + 18: $53+20-2$ |  | V | * |  |
| 84-18: 84-20+2 |  |  | V | * |
| 38+68: $38+70-2$ |  |  | $\checkmark$ | * |
| 95-78: $95-80+2$ |  |  | V | * |
| 58 + 32: $58+30+2$ |  |  | V | * |


| $64-32: 64-30-2$ |  |  | V | $*$ |
| :--- | :--- | :--- | :--- | :--- |
| $138+69: 138+70-1$ |  |  | V | $*$ |
| $405-399: 405-400+1$ |  |  | V | $*$ |
| $21 / 2+13 / 4: 21 / 2+2-1 / 4$ |  |  |  | V |
| $5.7+3.9: 5.7+4 .-0.1$ |  |  |  | V |
| $6.8-4.9: 6.8-5.0+0.1$ |  |  |  | V |

